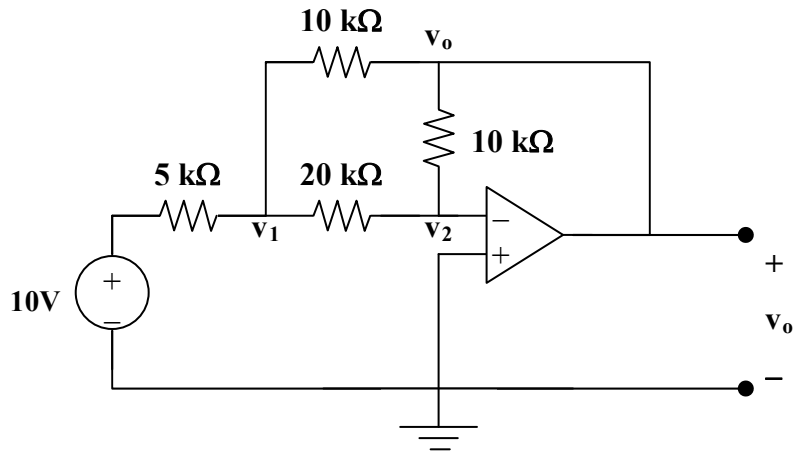


**Chapter 5, Solution 14.**

Transform the current source as shown below. At node 1,

$$\frac{10 - v_1}{5} = \frac{v_1 - v_2}{20} + \frac{v_1 - v_o}{10}$$



But  $v_2 = 0$ . Hence  $40 - 4v_1 = v_1 + 2v_1 - 2v_o \longrightarrow 40 = 7v_1 - 2v_o$  (1)

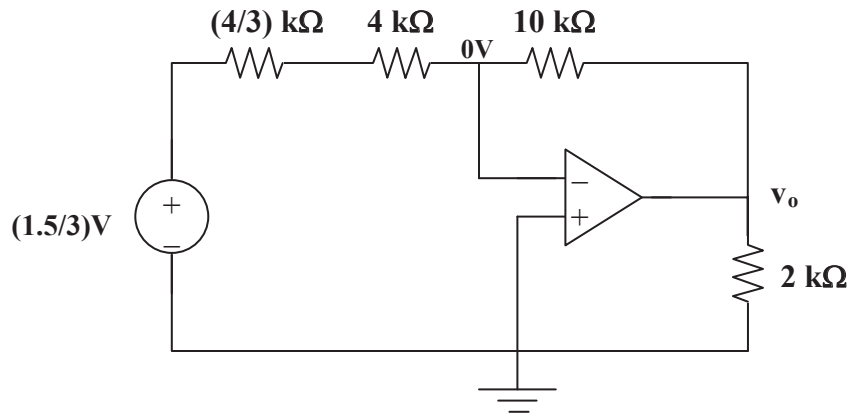
At node 2,  $\frac{v_1 - v_2}{20} = \frac{v_2 - v_o}{10}$ ,  $v_2 = 0$  or  $v_1 = -2v_o$  (2)

From (1) and (2),  $40 = -14v_o - 2v_o \longrightarrow v_o = -2.5V$

**Chapter 5, Solution 19.**

We convert the current source and back to a voltage source.

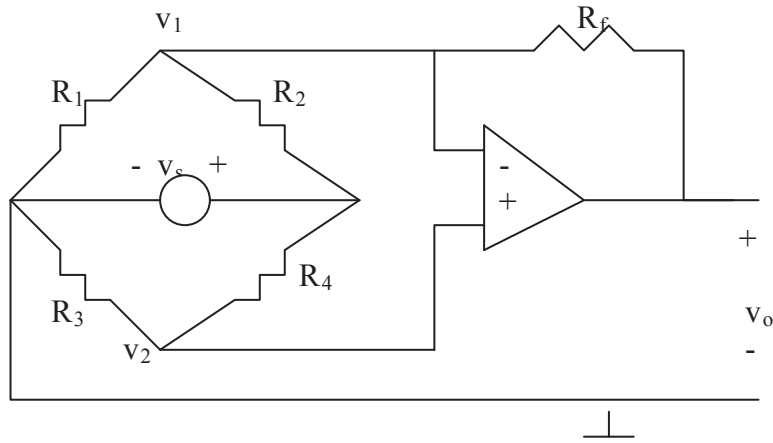
$$2 \parallel 4 = \frac{4}{3}$$



$$v_o = -\frac{10k}{\left(4 + \frac{4}{3}\right)k} \left(\frac{1.5}{3}\right) = -937.5 \text{ mV.}$$

$$i_o = \frac{v_o}{2k} + \frac{v_o - 0}{10k} = -562.5 \text{ } \mu\text{A.}$$

### Chapter 5, Solution 24



We notice that  $v_1 = v_2$ . Applying KCL at node 1 gives

$$\frac{v_1}{R_1} + \frac{(v_1 - v_s)}{R_2} + \frac{v_1 - v_o}{R_f} = 0 \quad \longrightarrow \quad \left( \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_f} \right) v_1 - \frac{v_s}{R_2} = \frac{v_o}{R_f} \quad (1)$$

Applying KCL at node 2 gives

$$\frac{v_1}{R_3} + \frac{v_1 - v_s}{R_4} = 0 \quad \longrightarrow \quad v_1 = \frac{R_3}{R_3 + R_4} v_s \quad (2)$$

Substituting (2) into (1) yields

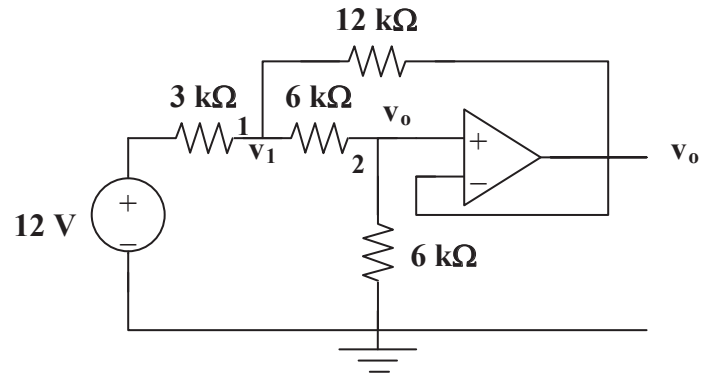
$$v_o = R_f \left[ \left( \frac{R_3}{R_1} + \frac{R_3}{R_f} - \frac{R_4}{R_2} \right) \left( \frac{R_3}{R_3 + R_4} \right) - \frac{1}{R_2} \right] v_s$$

i.e.

$$\underline{k = R_f \left[ \left( \frac{R_3}{R_1} + \frac{R_3}{R_f} - \frac{R_4}{R_2} \right) \left( \frac{R_3}{R_3 + R_4} \right) - \frac{1}{R_2} \right]}$$

### Chapter 5, Solution 31.

After converting the current source to a voltage source, the circuit is as shown below:



At node 1,

$$\frac{12 - v_1}{3} = \frac{v_1 - v_o}{6} + \frac{v_1 - v_o}{12} \longrightarrow 48 = 7v_1 - 3v_o \quad (1)$$

At node 2,

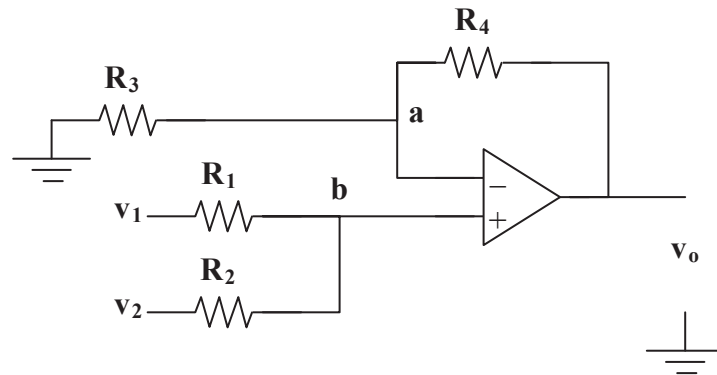
$$\frac{v_1 - v_o}{6} = \frac{v_o - 0}{6} = i_x \longrightarrow v_1 = 2v_o \quad (2)$$

From (1) and (2),

$$v_o = \frac{48}{11}$$

$$i_x = \frac{v_o}{6k} = 727.2\mu\text{A}$$

Chapter 5, Solution 44.



$$\text{At node b, } \frac{v_b - v_1}{R_1} + \frac{v_b - v_2}{R_2} = 0 \longrightarrow v_b = \frac{\frac{v_1}{R_1} + \frac{v_2}{R_2}}{\frac{1}{R_1} + \frac{1}{R_2}} \quad (1)$$

$$\text{At node a, } \frac{0 - v_a}{R_3} = \frac{v_a - v_o}{R_4} \longrightarrow v_a = \frac{v_o}{1 + R_4/R_3} \quad (2)$$

But  $v_a = v_b$ . We set (1) and (2) equal.

$$\frac{v_o}{1 + R_4/R_3} = \frac{R_2 v_1 + R_1 v_2}{R_1 + R_2}$$

or

$$v_o = \frac{(R_3 + R_4)}{R_3(R_1 + R_2)} (R_2 v_1 + R_1 v_2)$$

## Chapter 5, Solution 65

The output of the first op amp (to the left) is 6 mV. The second op amp is an inverter so that its output is

$$v_o' = -\frac{30}{10}(6\text{mV}) = -18\text{ mV}$$

The third op amp is a noninverter so that

$$v_o' = \frac{40}{40+8} v_o \quad \longrightarrow \quad v_o = \frac{48}{40} v_o' = \underline{\underline{-21.6\text{ mV}}}$$

**Chapter 5, Solution 73.**

The first stage is a noninverting amplifier. The output is

$$v_{o1} = \frac{50}{10}(1.8) + 1.8 = 10.8V$$

The second stage is another noninverting amplifier whose output is

$$v_L = v_{o1} = \mathbf{10.8V}$$

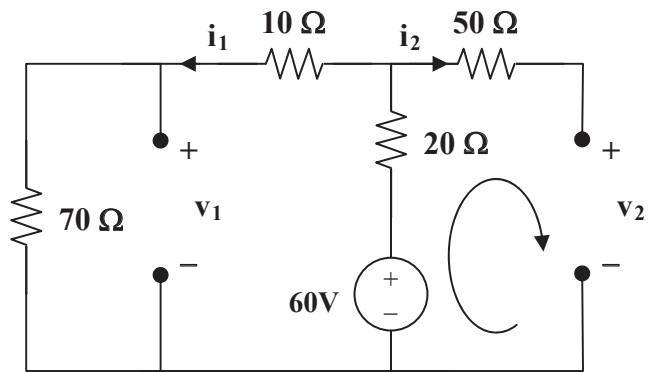
**Chapter 5, Solution 89.**

A **summer** with  $v_o = -v_1 - (5/3)v_2$  where  $v_2 = 6\text{-V battery}$  and an **inverting amplifier** with  $v_1 = -12v_s$ .



### Chapter 6, Solution 13.

Under dc conditions, the circuit becomes that shown below:



$$i_2 = 0, i_1 = 60/(70+10+20) = 0.6 \text{ A}$$

$$v_1 = 70i_1 = 42 \text{ V}, v_2 = 60 - 20i_1 = 48 \text{ V}$$

Thus,  $v_1 = 42 \text{ V}$ ,  $v_2 = 48 \text{ V}$ .

**Chapter 6, Solution 21.**

$$4\mu\text{F in series with } 12\mu\text{F} = (4 \times 12) / 16 = 3\mu\text{F}$$

$$3\mu\text{F in parallel with } 3\mu\text{F} = 6\mu\text{F}$$

$$6\mu\text{F in series with } 6\mu\text{F} = 3\mu\text{F}$$

$$3\mu\text{F in parallel with } 2\mu\text{F} = 5\mu\text{F}$$

$$5\mu\text{F in series with } 5\mu\text{F} = 2.5\mu\text{F}$$

Hence  $C_{\text{eq}} = \mathbf{2.5\mu\text{F}}$

**Chapter 6, Solution 25.**

(a) For the capacitors in series,

$$Q_1 = Q_2 \longrightarrow C_1 v_1 = C_2 v_2 \longrightarrow \frac{v_1}{v_2} = \frac{C_2}{C_1}$$
$$v_s = v_1 + v_2 = \frac{C_2}{C_1} v_2 + v_2 = \frac{C_1 + C_2}{C_1} v_2 \longrightarrow v_2 = \frac{C_1}{C_1 + C_2} v_s$$

Similarly,  $v_1 = \frac{C_2}{C_1 + C_2} v_s$

(b) For capacitors in parallel

$$v_1 = v_2 = \frac{Q_1}{C_1} = \frac{Q_2}{C_2}$$
$$Q_s = Q_1 + Q_2 = \frac{C_1}{C_2} Q_2 + Q_2 = \frac{C_1 + C_2}{C_2} Q_2$$

or

$$Q_2 = \frac{C_2}{C_1 + C_2} Q_s$$
$$Q_1 = \frac{C_1}{C_1 + C_2} Q_s$$

$$i = \frac{dQ}{dt} \longrightarrow i_1 = \frac{C_1}{C_1 + C_2} i_s, \quad i_2 = \frac{C_2}{C_1 + C_2} i_s$$

**Chapter 6, Solution 40.**

$$i = \begin{cases} 5t, & 0 < t < 2\text{ms} \\ 10, & 2 < t < 4\text{ms} \\ 30 - 5t, & 4 < t < 6\text{ms} \end{cases}$$

$$v = L \frac{di}{dt} = \frac{5 \times 10^{-3}}{10^{-3}} \begin{cases} 5, & 0 < t < 2\text{ms} \\ 0, & 2 < t < 4\text{ms} \\ -5, & 4 < t < 6\text{ms} \end{cases} = \begin{cases} 25, & 0 < t < 2\text{ms} \\ 0, & 2 < t < 4\text{ms} \\ -25, & 4 < t < 6\text{ms} \end{cases}$$

At  $t = 1\text{ms}$ ,  $v = \mathbf{25\text{ V}}$

At  $t = 3\text{ms}$ ,  $v = \mathbf{0\text{ V}}$

At  $t = 5\text{ms}$ ,  $v = \mathbf{-25\text{ V}}$

**Chapter 6, Solution 53.**

$$L_{\text{eq}} = 6 + 10 + 8 \parallel [5 \parallel (8 + 12) + 6 \parallel (8 + 4)]$$

$$= 16 + 8 \parallel (4 + 4) = 16 + 4$$

$$L_{\text{eq}} = \mathbf{20 \text{ mH}}$$

**Chapter 6, Solution 53.**

$$L_{\text{eq}} = 6 + 10 + 8 \parallel [5 \parallel (8 + 12) + 6 \parallel (8 + 4)]$$

$$= 16 + 8 \parallel (4 + 4) = 16 + 4$$

$$L_{\text{eq}} = \mathbf{20 \text{ mH}}$$

**Chapter 6, Solution 65.**

$$(a) \quad w_5 = \frac{1}{2} L_1 i_1^2 = \frac{1}{2} \times 5 \times (4)^2 = \mathbf{40 \text{ J}}$$

$$w_{20} = \frac{1}{2} (20)(-2)^2 = \mathbf{40 \text{ J}}$$

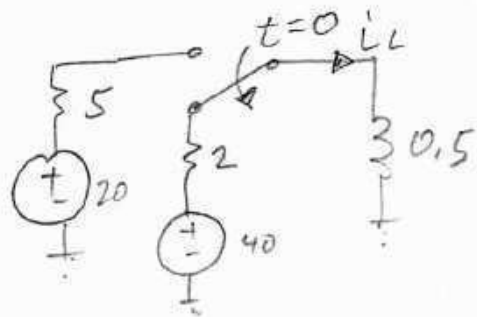
$$(b) \quad w = w_5 + w_{20} = \mathbf{80 \text{ J}}$$

$$(c) \quad i_1 = \frac{1}{L_1} \int_0^t -50e^{-200t} dt + i_1(0) = \frac{1}{5} \left( \frac{1}{200} \right) \left( 50e^{-200t} \times 10^{-3} \right) \Big|_0^t + 4 \\ = \mathbf{[5 \times 10^{-5} (e^{-200t} - 1) + 4] \text{ A}}$$

$$i_2 = \frac{1}{L_2} \int_0^t -50e^{-200t} dt + i_2(0) = \frac{1}{20} \left( \frac{1}{200} \right) \left( 50e^{-200t} \times 10^{-3} \right) \Big|_0^t - 2 \\ = \mathbf{[1.25 \times 10^{-5} (e^{-200t} - 1) - 2] \text{ A}}$$

$$(d) \quad i = i_1 + i_2 = \mathbf{[6.25 \times 10^{-5} (e^{-200t} - 1) + 2] \text{ A}}$$

# Supplemental 1



Final conditions:

$$\frac{t=0^-}{I_L(0^-) = 4A}$$

$$V_L(t) = 0V$$

$$\frac{t=0^+}{I_L = 4A}$$

$$V_L = 32V$$

$$\frac{t=\infty}{I_L = 20A}$$

$$V_L = 0$$

$$\text{KVL: } -40 + I_L 2 + \frac{1}{2} \frac{dI_L}{dt} = 0$$

$$\Rightarrow \frac{1}{4} I_L' + I_L = 20$$

$$\Rightarrow \tau = \frac{1}{4} \Rightarrow i_H(t) = C e^{-t/\tau}$$

$$\text{General solution: } i(t) = C e^{-t/\tau} + i_p \Rightarrow i_p = 20A @ t = \infty$$

$$i(t) = C e^{-t/\tau} + 20$$

$$\Rightarrow i(0^+) = 4 = C e^{-t/\tau} + 20 \Rightarrow -16 = C$$

$$\Rightarrow \boxed{i(t) = 20 - 16 e^{-4t}}$$



